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5 **FRP REPAIR & STRENGTHENING OF DAMAGED END REGIONS OF**  
6 **PRESTRESSED BEAMS**  
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15  
16 **ABSTRACT**  
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18 *A common serviceability problem in prestressed concrete (PC) bridges in the*  
19 *Midwest states is the deterioration/damage of the beams' end regions, which*  
20 *can be attributed to reasons like excessive thermal distortion in fascia beams*  
21 *or corrosion of steel reinforcement. Studies have shown that inadequate*  
22 *maintenance of expansion joints located at the beam end leads to excessive*  
23 *leakage of deicing materials and water onto the beam end, causing severe*  
24 *corrosion damage to shear reinforcement and also cracking and spalling of*  
25 *concrete. Another important factor that accelerates the rate of deterioration is*  
26 *the freeze-thaw cycles experienced by the concrete. To avoid the complete*  
27 *replacement of the beams with damaged ends, there is a need for effective*  
28 *repair measures that can restore/maintain the structural integrity and*  
29 *serviceability of these beams. This study focuses on exploring the effectiveness*  
30 *of conventional and innovative repairing methods to restore the shear*  
31 *capacity of PC beams with severely damaged end regions using experimental*  
32 *and numerical approaches. The use of Fiber Reinforced Polymer (FRP)*  
33 *laminates for repair was explored experimentally in addition to exploring*  
34 *numerically with FE modeling an innovative repair concept using prestressed*  
35 *Shape Memory Alloy (SMA) wires. Three half-scale PC I-girders are cast with*  
36 *reduced area stirrups in the end regions to represent damage. Various shear*  
37 *FRP laminate schemes are experimentally tested, including several which*  
38 *utilize longitudinal FRP strips to prevent premature laminate debonding from*  
39 *the concrete substrate. In the FE model curved prestressed SMA wires are*  
40 *embedded in the concrete cover to help restore the girder's shear strength.*  
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43 **Keywords:** End region, Repair, Prestressed concrete, Fiber reinforced polymer, Shape  
44 memory alloy

45 **INTRODUCTION**

46 In the Northeast and Midwest of United States, over 58,000 bridges have been deemed  
47 structurally deficient and faced replacing, rehabilitation and repair<sup>1</sup>. Harsh climates in these  
48 regions caused deterioration in concrete structures at an accelerated rate. One specific  
49 problem that plagues bridges is the deterioration of the beam's end regions due to failure of  
50 expansion joint which allows water containing deicing salts to flow onto the beam ends, as  
51 shown in Figure 1(a). Another factor causing the damage at beam's end region is freezing  
52 and thawing cycles which result in scaling and spalling of the cover concrete. This does not  
53 only impact the appearance of the girders and increase the difficulty of inspection, but also  
54 directly expose the steel reinforcement to chlorides and accelerate the rate of corrosion of  
55 steel reinforcement and spalling of concrete. Due to the localized nature of this damage, the  
56 primary concern is shear failure. Traditionally mortar is utilized to repair girder's end region  
57 as shown in Figure 1(b). However, no studies were ever conducted to quantify the shear  
58 capacity gained by using mortar alone.

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61 Fig. 1 End region of prestressed girder: (a) end damage of girder; (b) typical mortar repair of  
62 girder end  
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64 Fiber reinforced polymer (FRP) laminates or sheets have been used as an effective  
65 repair and rehabilitation material over the past two decades because of its high strength to  
66 weight ratio and good corrosion resistance. One method of applying the laminates to the  
67 concrete surface is through a wet layup approach<sup>2</sup>, in which the resin serves to saturate the  
68 fibers and bond the sheet to concrete surface. Due to its flexibility, FRP laminates could be  
69 added as external shear reinforcement to a girder through wet layup approach.

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71 It has been proved that externally bonded FRP laminate could repair and strengthen  
72 the flexural behavior of concrete bridges<sup>3,4,5,6</sup>. More recently, externally bonded FRP in the  
73 form of U-wraps or bonded face plies has been proved to be effective in strengthening  
74 girders in shear<sup>7</sup>. However, there is limited studies focusing on the effectiveness of FRP  
75 repair combined with conventional mortar repair in short shear span.

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77 This paper presents an experimental and numerical study on the application of FRP  
78 composites in repairing and retrofitting damaged ends of prestressed girders. Three-point  
79 bending tests were performed on small-scale girders repaired with mortar and FRP laminates  
80 systems. In addition, a full-scale girder finite element model was generated to explore the

81 effectiveness of repair using FRP laminates and an innovative repair method using thermally-  
 82 prestressed shape memory alloy (SMA) curved wires.

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85 **FLXURAL TESTING OF SMALL-SCALE GIRDERS**

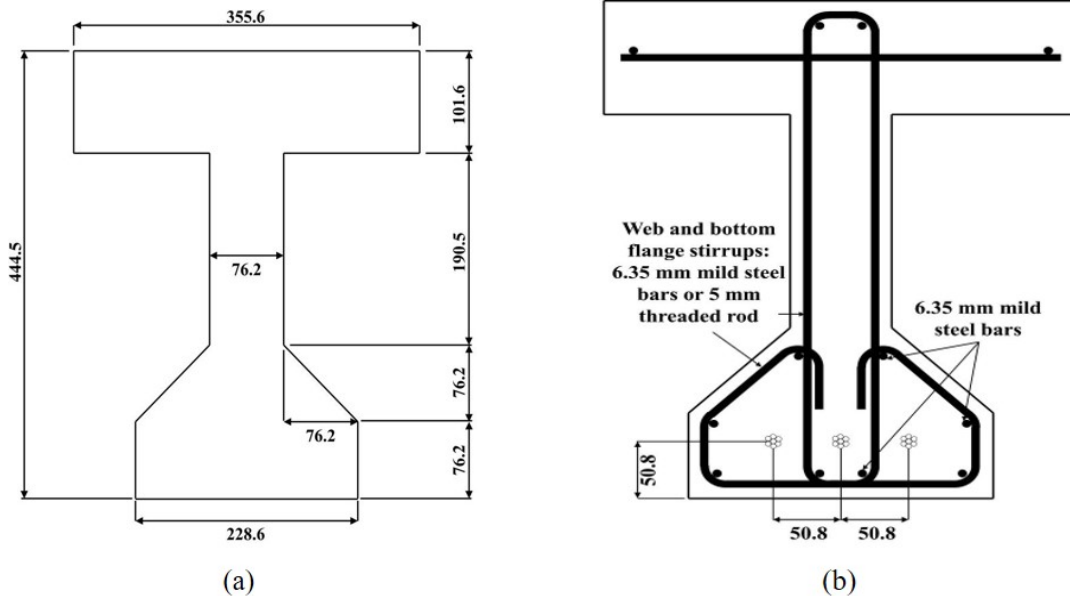
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87 **BEAM DESIGN AND CASTING**

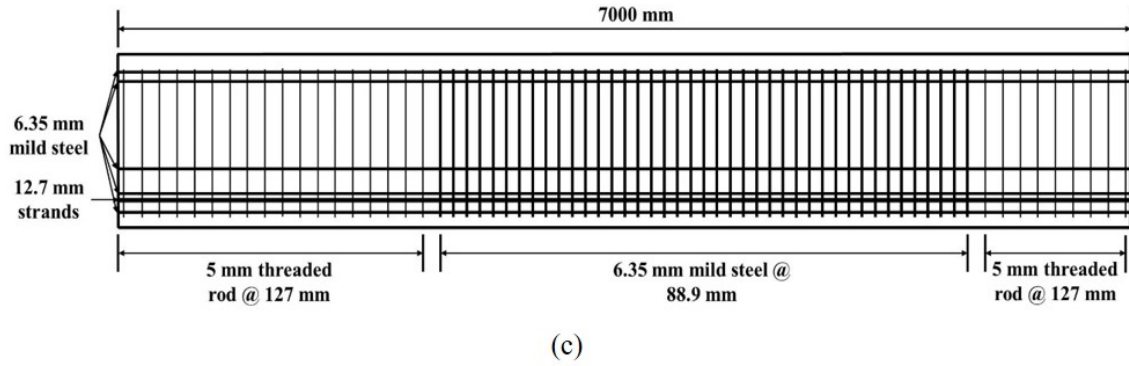
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89 Three 23-ft (7-m) long small-scale PC beams were cast in the laboratory. The details of cross  
 90 section and steel reinforcement are shown in Figure 2(a)-(c). The cross section of the beam  
 91 was scaled to half size of AASHTO Type II I-girder and a top flange was cast on top to  
 92 increase the flexural capacity of the beams. The compressive strength of the concrete at 28-  
 93 day was 6.94 ksi (48.1 MPa). Three 0.5 in. (12.7 mm) diameter 7-wire strands with elastic  
 94 modulus equal to 28700 ksi (197.9 GPa) and ultimate strength equal to 270 ksi (1862 MPa)  
 95 were prestressed to 178 ksi (1234 MPa) (66% of ultimate strength). All the longitudinal and  
 96 shear reinforcement had same yield strength equal to 60 ksi (414 MPa). At end region of the  
 97 beam, the diameter of stirrups was reduced to 0.2 in. (5 mm) and spacing was increased to  
 98 5.0 in. (127 mm) to promote and facilitate shear failure.

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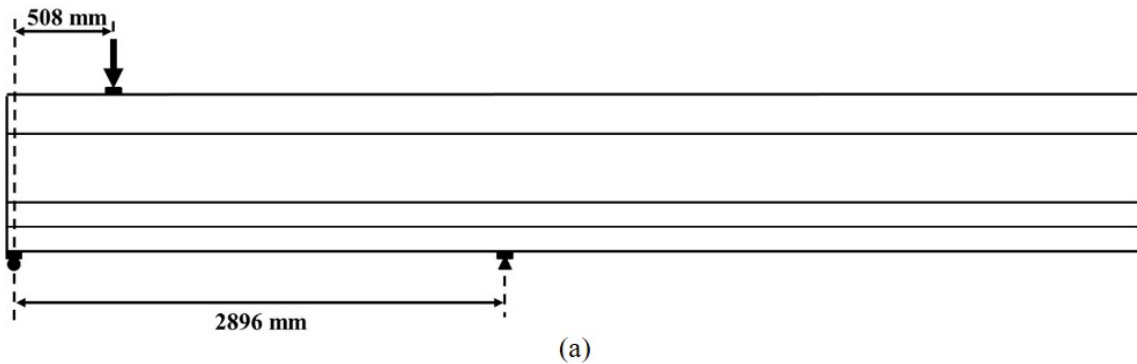


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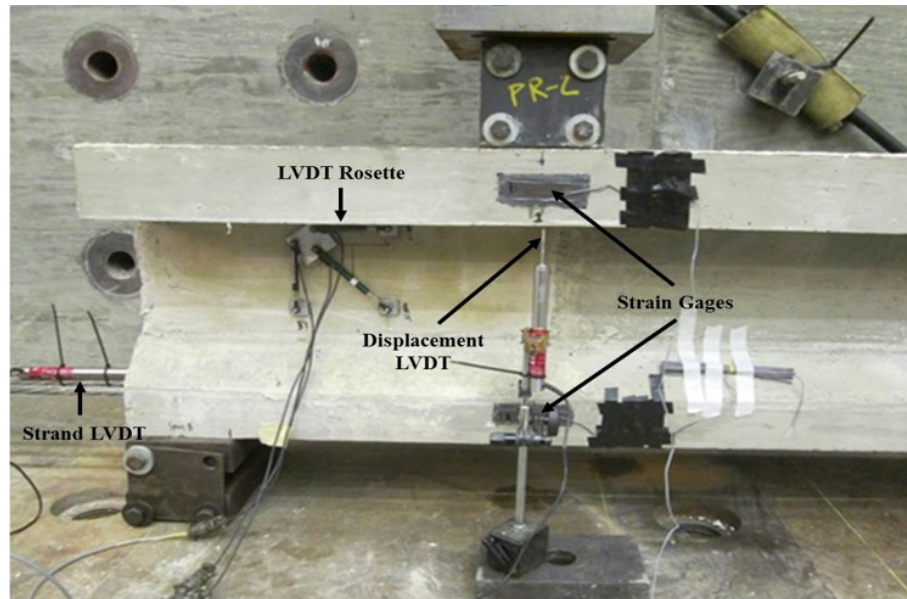
Fig. 2 Beam design (in mm): (a) cross section dimensions; (b) reinforcement details; (c) elevation view

TEST SETUP

Three-point bending tests were carried out to test the shear capacity of the beams. The test setup used is illustrated in Figure 3(a). To represent the localized nature of damage, a low span-to-depth ratio equal to 1.3 the beam’s effective depth ( $d_p$ ) was adopted. The depth to the prestressing strand ( $d_p$ ) was 15.5 in. (394 mm), thus, the distance from the center of the support to the loading point was 20.0 in. (508 mm).



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(b)

Fig. 3 Test setup: (a) three-point bending test; (b) beam instrumentation

The instrumentations used for the tests are shown in Figure 3(b). Three LVDTs placed at 0°, 45° and 90° formed a rosette configuration to measure the principal strain in the shear span. One vertical LVDT was placed beneath top flange to measure the deflection of the beam during loading. One LVDT was clamped to prestressing strand to monitor the end-slip of the strands. To measure compressive and tensile strains of the beam, two strain gages were attached to top and bottom flange of the beam. The test was controlled by displacement and load was applied by 100-kip (445-kN) capacity actuator.

DAMAGE AND REPAIR OF BEAM ENDS

The test matrix is shown in Table 1. There were five tests in total including control, damage, mortar repair and two FRP repair tests. The compressive strength of mortar used in repair is listed in the table.

Table 1. Test matrix

Test	Cover Damage	Mortar Repair	FRP Repair	Mortar Compressive Strength, ksi (MPa)
Control	--	--	--	--
Damaged	X	--	--	--
Mortar	X	X	--	3.39 (23.4)
GFRP	X	X	X	4.21 (29.0)
CFRP	X	X	X	3.99 (27.5)

133 To represent the damage to the end region of the girder in the field, removal of  
 134 concrete cover with a depth equal to 0.5 in. (12.7 mm) was applied to the web within shear  
 135 span on both sides. The beam web after removal of concrete cover is shown Figure 4.  
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137  
 138 Fig. 4 Beam web after cover removal  
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140 After cover was removed, the surface was vacuumed and air blasted. Afterwards a fast  
 141 setting mortar was mixed and applied to the beam web. In addition to mortar repair,  
 142 externally bonded glass-FRP (GFRP) and carbon-FRP (CFRP) laminates were also applied  
 143 on the top of the cover mortar. The dimensions of FRP laminate systems used in test and the  
 144 material properties are summarized in Table 2.  
 145

146 Due to the presence of bearing plate in the test and limited access to the bottom of the  
 147 girder in the field, externally bonded U-wrap was not applicable. Thus, this study adopted  
 148 bonded face ply FRP repair schemes. The FRP laminates started from the top of the beam  
 149 web and terminated at the bottom edge of the bottom flange. Eight 6 in. (152.4 mm) wide  
 150 panels of shear FRP reinforcement with vertical fiber orientation were attached to the beams  
 151 using epoxy resin. Due to relatively low stiffness and strength of GFRP compared to CFRP,  
 152 more plies of GFRP were utilized to achieve similar load in FRP for similar effective strain.  
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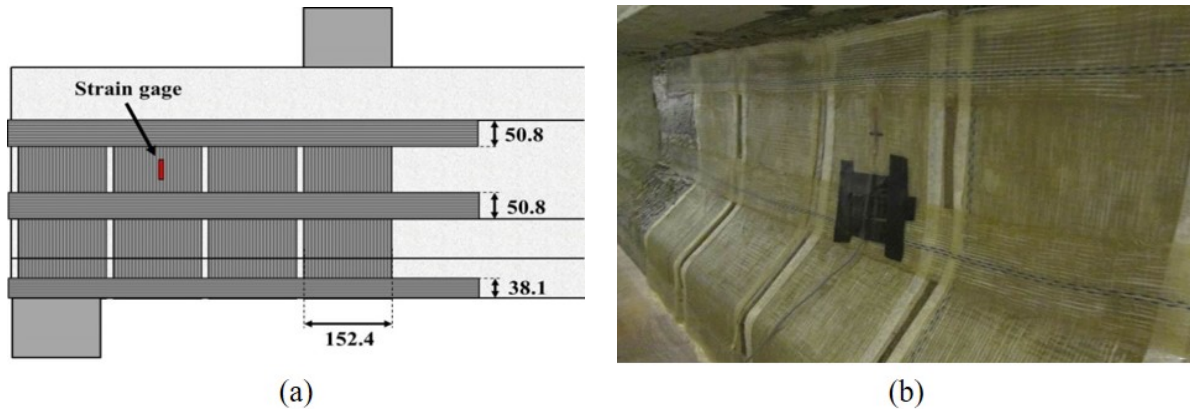
154 Table 2. Test matrix

<b>Material</b>	<b>Ply Thickness, in. (mm)</b>	<b>Shear Reinforcement Details</b>	<b>Elastic Modulus ksi, (GPa)</b>	<b>Tensile Strength ksi, (MPa)</b>	<b>Tensile strain, in./in. (mm/mm)</b>
GFRP laminate	0.050 (1.27)	8 x 6 in. (152.4 mm) x 3 plies	3219 (22.2)	57.8 (399)	0.018
CFRP laminate	0.049 (1.24)	8 x 6 in. (152.4 mm) x 1 ply	13300 (91.7)	147.9 (1020)	0.011

155 To improve the bond between FRP laminates and concrete, additional FRP strips  
 156 were used as longitudinal anchors as shown in Figure 5(a). Three FRP strips were placed at  
 157 the top of the web, bottom of the web and along the bottom edge of the bottom flange. To  
 158 increase development of the anchors at beam end, the anchors were wrapped around beam  
 159 end and continued along the other side. After laminates and anchors were attached, a strain  
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161 gage was placed vertically on the FRP reinforcement close to the center of the shear span.  
 162 Eventually repair using shear FRP reinforcement was shown in Figure 5(b).  
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164  
 165 Fig. 5 FRP repair design: (a) FRP repair dimensions (mm); (b) FRP panels with longitudinal  
 166 anchors  
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168 RESULTS AND DISCUSSION

169  
 170 The test results including peak load, secant stiffness at deflection equal to 0.079 in. (2 mm),  
 171 slip of strand, max. principal strain and max. FRP strain are summarized in Table 3. The  
 172 failure modes of the beams were governed by either shear cracking along the diagonal  
 173 compression strut as in the cases of Control, Damaged, and Mortar specimens or debonding  
 174 of FRP reinforcement as in the cases of GFRP and CFRP specimens. The load-deflection  
 175 curves are depicted in Figure 6.  
 176

177 Table 3. Test results

Specimen	Peak load, kips (kN)	% of Control peak load	% of Control stiffness	Strand slip at peak load, in. (mm)	Max. principal strain in web at peak load, in./in. (mm/mm)	Max. FRP strain, in./in. (mm/mm)
Control	63.6 (282.9)	100.0	100.0	0.071 (1.81)	0.0153	--
Damaged	46.4 (206.4)	73.0	75.9	0.018 (0.46)	0.0063	--
Mortar	51.6 (229.5)	81.1	78.9	0.020 (0.51)	0.0062	--
GFRP	64.9 (288.7)	102.0	74.4	0.080 (2.03)	0.0108	0.0012
CFRP	76.0 (338.0)	119.5	106.0	0.052 (1.33)	0.0065	0.0034

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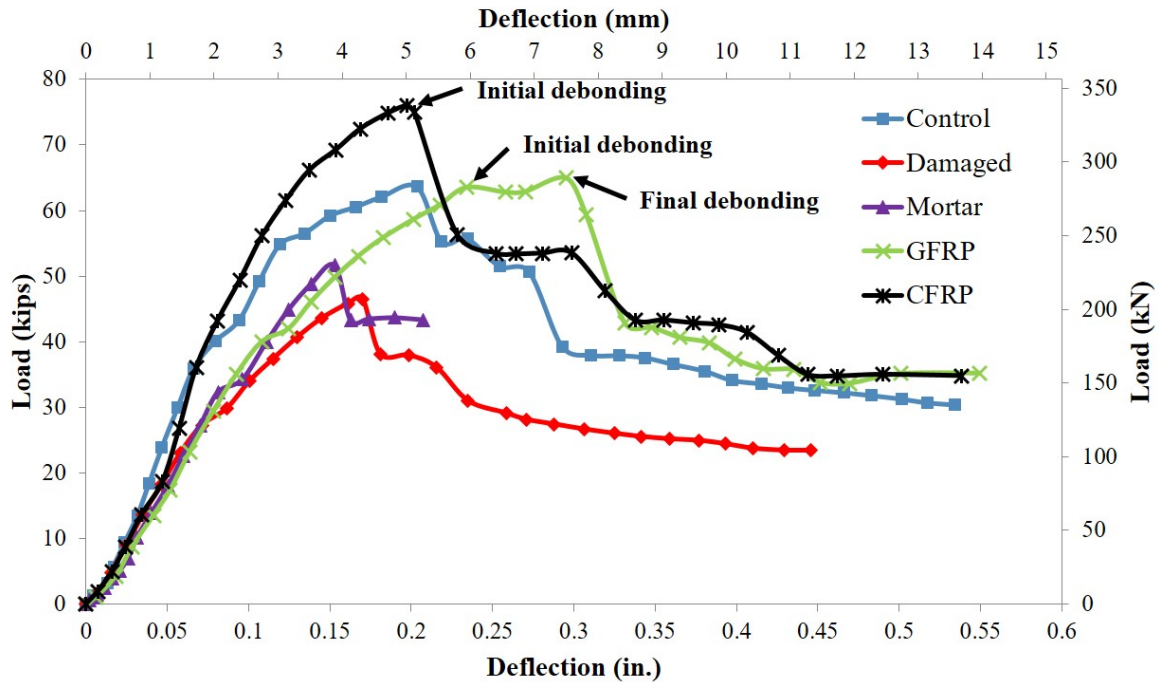


Fig. 6 Load-deflection curves

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As shown in Figure 6, removal of concrete cover resulted in 27.0% and 24.1% reduction in peak load and stiffness respectively. Mortar repaired specimen reached 81.1% of the peak load and 78.9% of the stiffness of the Control specimen. The max. principal strain of Mortar specimen was lower than Control and Damaged specimen, which indicated that additional mortar didn't fully engage with the core concrete. Two reasons could contribute to this issue: 1) the compressive strength of mortar was lower than that of beam concrete; 2) the cold joint existed between the exposed core concrete and mortar repair. At this interface, reduced aggregate interlock diminishes the strength recovery effect of the mortar repair. Such phenomenon is also suggested by the cracking patterns shown in Figure 7. The shear cracks of Control case propagate directly from the support to the loading plate while the shear cracks of Mortar case travel along the junction between web and bottom flange before proceeding up through the web.



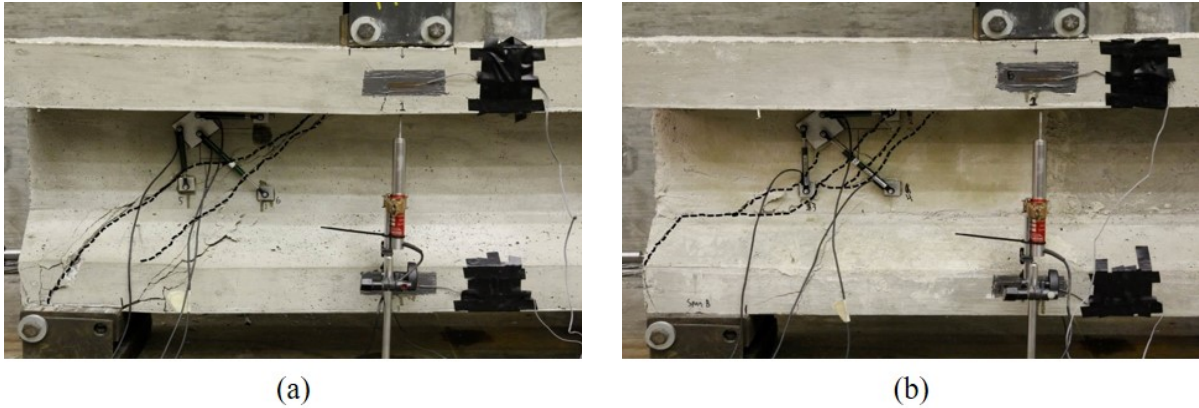
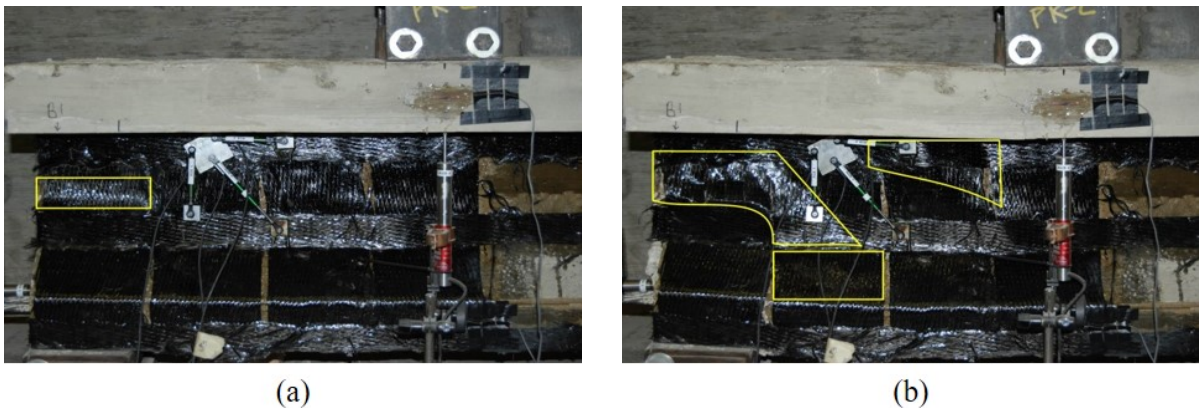


Fig. 7 Shear crack patterns: (a) Control case; (b) Mortar repair case

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With respect to FRP repair cases, both CFRP and GFRP repairs proven to be capable to restore the peak load of the beams. CFRP and GFRP tests reached 119.5% and 102.0% of the peak load of the Control test, respectively. However, only CFRP restored the stiffness of the beam, where CFRP test reached 106.0% of the stiffness of the Control specimen. The debonding patterns for both CFRP and GFRP are illustrated in Figure 8. From Figure 8(a), it is observed that in CFRP test debonding initiated in the endmost shear FRP panel and propagated further into adjacent panel. Due to the longitudinal anchors, complete delamination of CFRP laminates was prevented, as shown in Figure 8(b). While in GFRP test, debonding first occurred at web/bottom flange junction (see Figure 8(c)) and proceeded through the whole web and eventually complete debonding of GFRP sheets in second and third panels was observed (see Figure 8(d)). The ineffectiveness of the anchors in GFRP case can be attributed to the increased thickness of the shear FRP. Three plies of GFRP laminates reduced contact area between anchors and concrete in the 0.5 in. (12.7) mm gap between shear panels and sufficient bond was not provided to avoid complete delamination.



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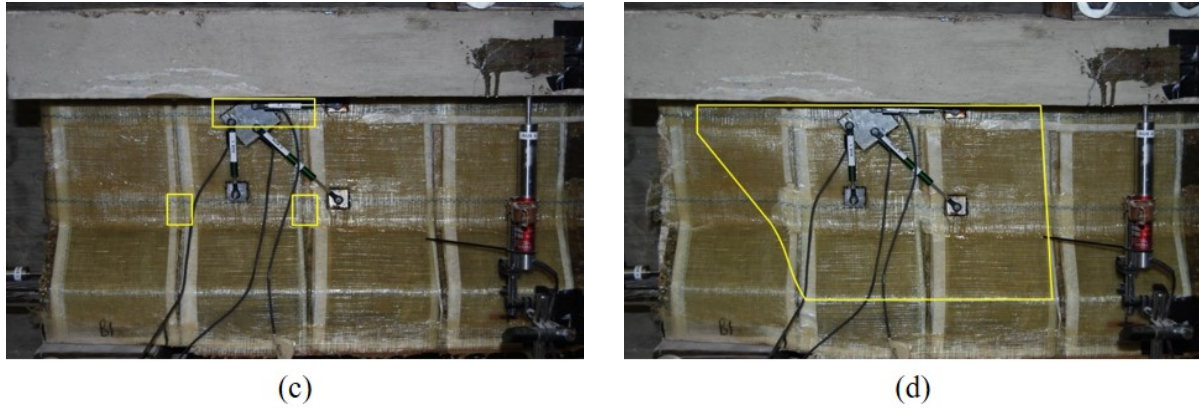


Fig. 8 FRP laminates debonding patterns: (a) CFRP: initial debonding; (b) CFRP: final debonding; (c) GFRP: initial debonding; (d) GFRP: final debonding

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## FINITE ELEMENT ANALYSIS

### MODEL DESCRIPTION AND CALIBRATION

A prestressed concrete (PC) I-girder from experimental tests performed by Andrawes and Pozolo<sup>8</sup> was utilized in the Finite Element Analysis (FEA) of this work<sup>8</sup>. The I-girder model included several geometrical parts: high strength prestressed strands, mild steel rebars and stirrups, concrete girder and loading/support plates. The details of the cross section of the PC I-girder is depicted in Figure 9. To reduce computational demand, only half of the I-girder cross section is modeled with a symmetric boundary condition defined on the inner face of the girder. Details about size and location of mild steel rebars and stirrups could be found in Andrawes and Pozolo's work<sup>9</sup>.

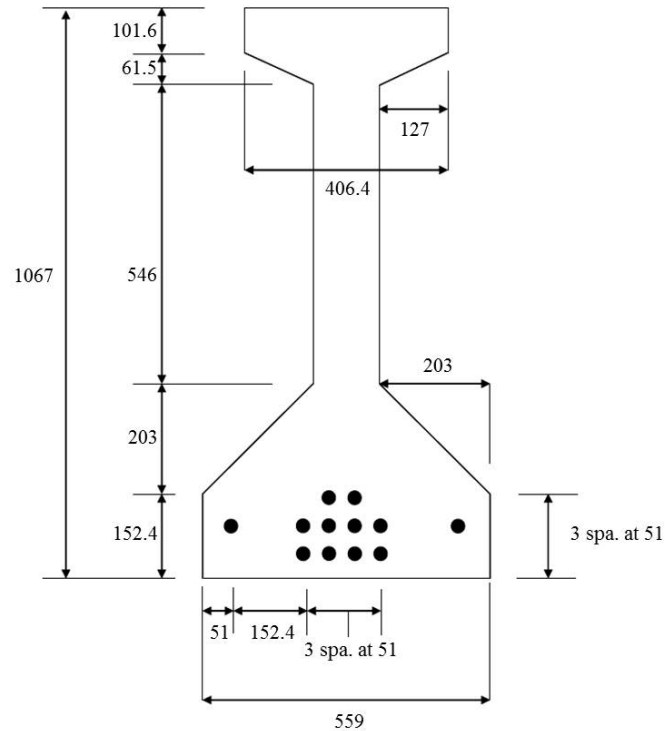
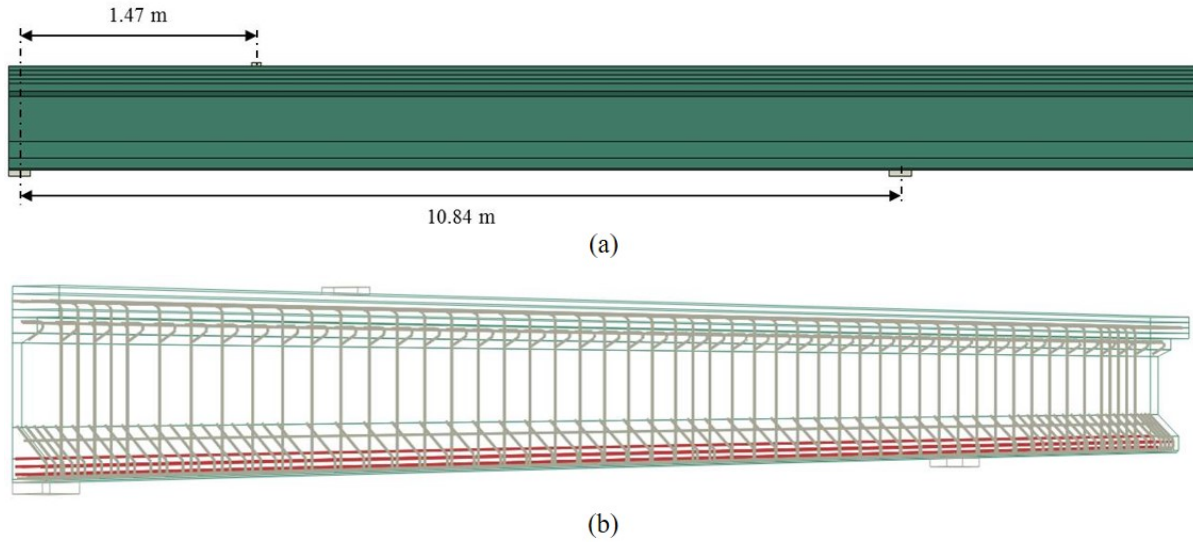


Fig. 9 Cross section of I-girder, in mm

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 235 The mild steel rebar and stirrups have a yield strength of 60 ksi (413.8 MPa) and  
 236 elastic modulus of 29000 ksi (200 GPa). The high strength prestressed strands have a cross  
 237 section of 0.153 in.<sup>2</sup> (98.7 mm<sup>2</sup>), with elastic modulus equal to 28700 ksi (197.9 GPa) and  
 238 ultimate strength equal to 270 ksi (1862 MPa). The mild steel rebars and stirrups and  
 239 prestressing strands were modeled using T3D2 2-node linear 3-D truss elements because  
 240 those elements are only subjected to tension and compression. Prestressing was applied to the  
 241 strands by imposing a negative predefined temperature field and the thermal expansion  
 242 coefficient was chosen so that an effective prestress reached approximately 165 ksi (1140  
 243 MPa). The concrete has a compressive strength equal to 6.06 ksi (41.8 MPa). The  
 244 support/loading plates have the same material property as the mild steel. Both concrete girder  
 245 and support/loading plates were modeled using C3D8 8-nodel linear brick elements.

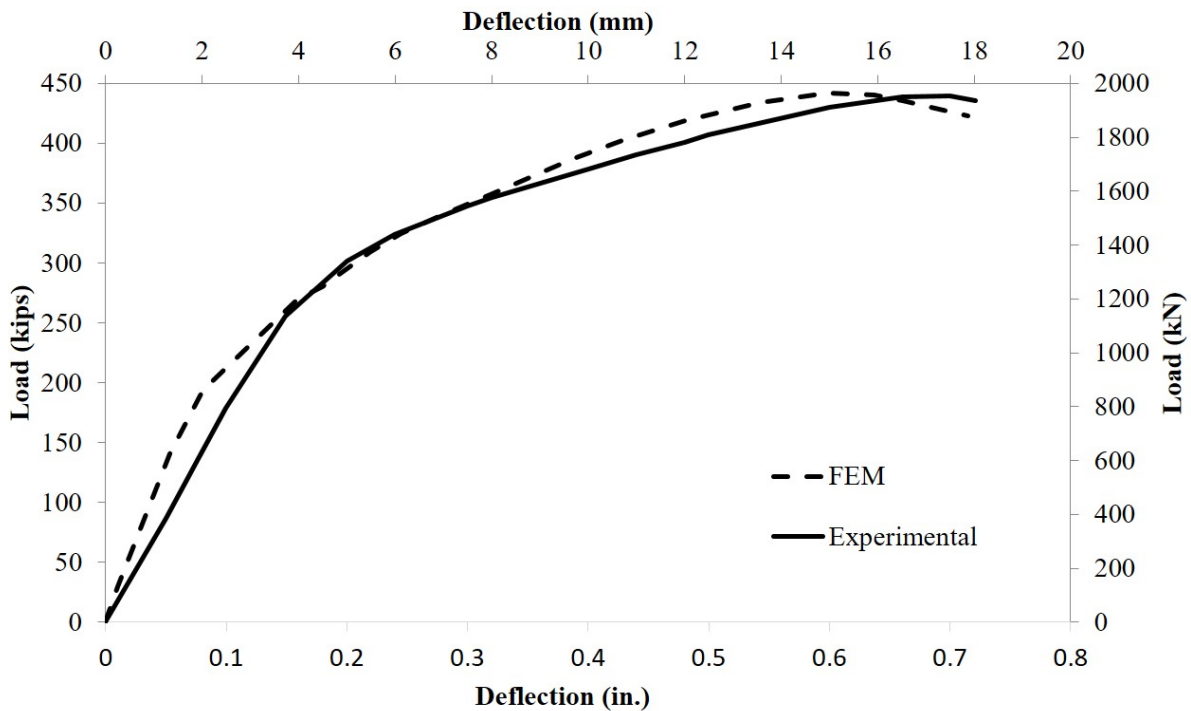
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 247 A three-point bending test was performed using the same test setup of Test 7 in  
 248 Andrawes and Pozolo's work<sup>8</sup>, which has a shear span of 57.9 in. (1.47 m) and a support-to-  
 249 support distance of 427 in. (10.84 m). The test setup and model assembly are illustrated in  
 250 Figure 10. The deflection was measured under the point of loading. The load-deflection  
 251 curve is shown in Figure 11. Although the FE model showed slightly higher initial stiffness  
 252 than test result, the load-deflection curve showed relatively good match.  
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Fig. 10 Model assembly: (a) Test setup of three-point bending test; (b) view of internal reinforcement



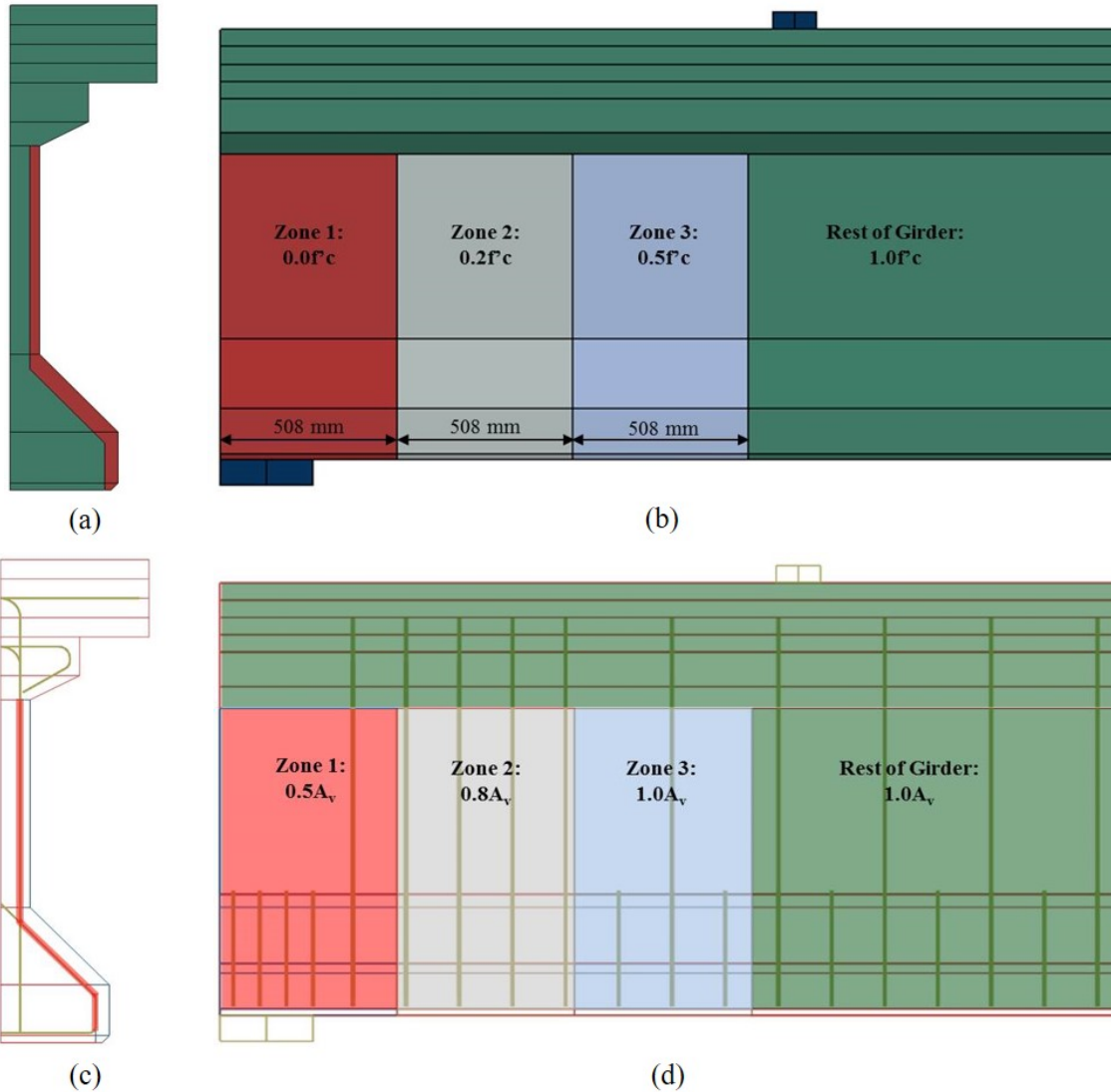
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Fig. 11 Load-deflection curve

DAMAGE AND REPAIR ANALYSIS

264 The damage to the beam end is mainly governed by the cracking/spalling of concrete cover  
265 and corrosion of steel reinforcement. To simulate these damages, both the concrete property  
266 of web cover and steel property of stirrups are reduced. Damage progression is adopted to

267 represent the real damage situation in the field, which is the region away from beam end  
 268 experienced less severe damage. As shown in Figure 12(b), the concrete cover within shear  
 269 span is divided into three 20 in. (508 mm) regions and had different properties. The region  
 270 (Zone 1) close to the beam end has  $0.0f'_c$ .  $0.2f'_c$  and  $0.5f'_c$  are assigned to Zone 2 and Zone 3  
 271 respectively. Figure 12 (d) illustrates the damage progression for vertical stirrups.  
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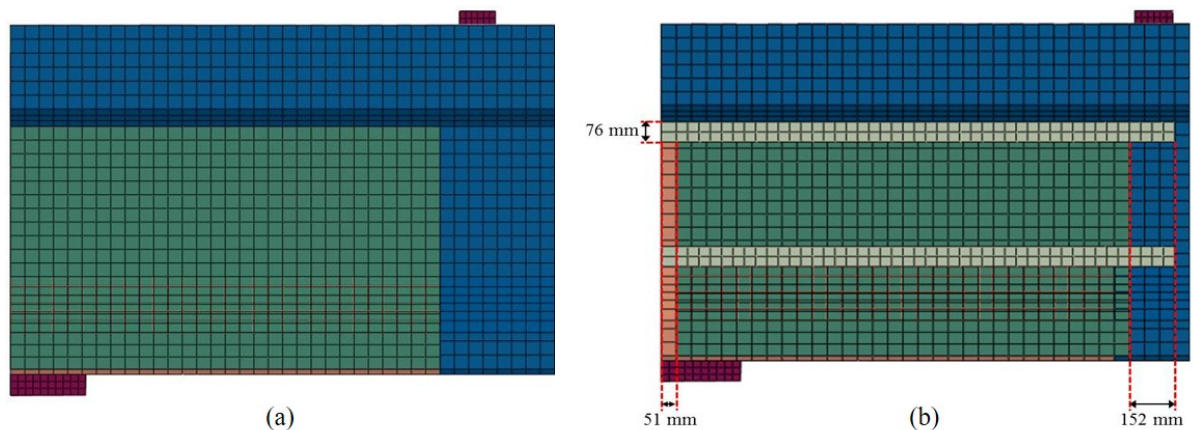
275 Fig. 12 Progressive end region damage scheme: (a) cover damage profile; (b) cover damage  
 276 zones; (c) stirrups damage profile; (d) stirrups damage zones  
 277

278 After the damage is introduced, repair technique is applied. The first repair case is  
 279 repair using mortar only. The compressive strength of mortar in early set stage tends to be in  
 280 the range of 2.9-4.35 ksi (20-30 MPa) and the cold joint between mortar and existing  
 281 concrete might diminish the contribution of mortar to restore the shear capacity of the girder.  
 282 Thus, the strength of mortar used in the model was approximately 3.03 ksi (20.9 MPa). As a



283 result, the cover concrete strength of Zone 1 and Zone 2 is increased to  $0.5f'_c$  while the cover  
 284 concrete strength of Zone 3 remains the same.

285 In addition to mortar repair, two FRP repair systems consisting of externally bonded  
 286 FRP laminates and prestressed SMA wires are investigated in this study. Due to its high  
 287 strength, CFRP laminate is utilized as additional shear reinforcement. One ply of CFRP  
 288 laminate covered the whole three damaged zones within shear span. The bond between shear  
 289 FRP reinforcement and mortar is simulated by using COH3D8 8-node three-dimensional  
 290 cohesive element. Additional two longitudinal strips with width equal to 3 in. (76 mm) serve  
 291 as anchors to improve the bond between sheet and mortar and delay the delamination. A  
 292 bond length of 2 in. (51 mm) at beam end and 6 in. (152 mm) extension past shear panel  
 293 would ensure sufficient development of those. Repair with externally bonded CFRP  
 294 laminates are shown in Figure 13. Properties for CFRP composite are from manufacturer's  
 295 data<sup>10</sup>.  
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 298 Fig. 13 CFRP repair scheme: (a) CFRP (Zone 1 to Zone 3); (b) CFRP-wa (with anchors)  
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300 To address the concern which many bridge engineers express regarding recovery of  
 301 the already distressed regions of the beam with external FRP laminates, which makes future  
 302 inspection quite difficult, a new repair approach using embedded prestressed wires was  
 303 explored numerically. Due to the ease and low labor required for prestressing shape memory  
 304 alloy (SMA) wires<sup>11</sup>, they were considered in this exploratory study. As illustrated in Figure  
 305 14, previous studies showed that 0.079 in. (2 mm) -diameter SMA wire with 6.2% prestrain  
 306 could produce considerable recovery stress (prestress) simply through heating. This prestress  
 307 will be maintained at a wide range of ambient temperature.  
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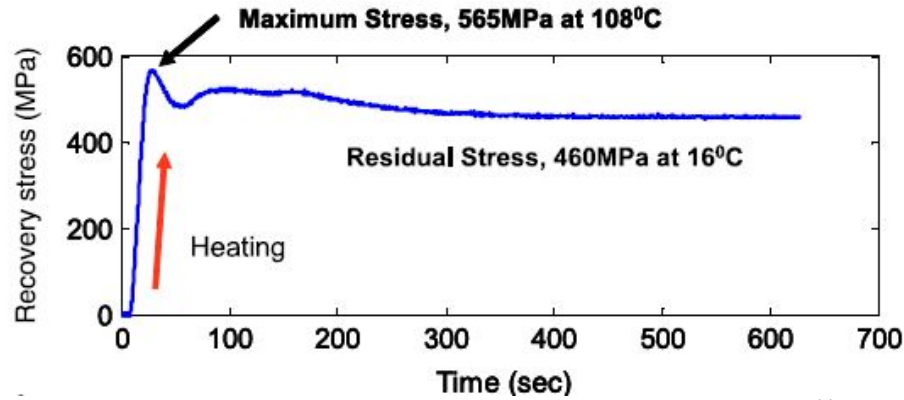


Fig. 14 Recovery stress developed in SMA during heating<sup>11</sup>

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By making use of this unique characteristic of SMA, embedding small diameter curved SMA wires (see Figure 15) into concrete cover of the short shear span region would generate sufficient stress in the web to improve the stiffness and shear strength and to control the crack propagation in this relatively limited-space region. Curved SMA wire with 18 in. (457 mm) straight legs are embedded. The SMA wire has cross section area of 0.098 in.<sup>2</sup> (63.2 mm<sup>2</sup>) (20 wires of 0.079 in. (2 mm) diameter) and spacing of 4 in. (102mm), which is approximately 23% of strength-wise equivalent area of CFRP laminate. Another case with same spacing and section area of 0.049 in.<sup>2</sup> (31.6 mm<sup>2</sup>) (10 wires of 0.079 in. (2 mm) diameter), which is approximately 12% of strength-wise equivalent area of CFRP laminate, is also explored.

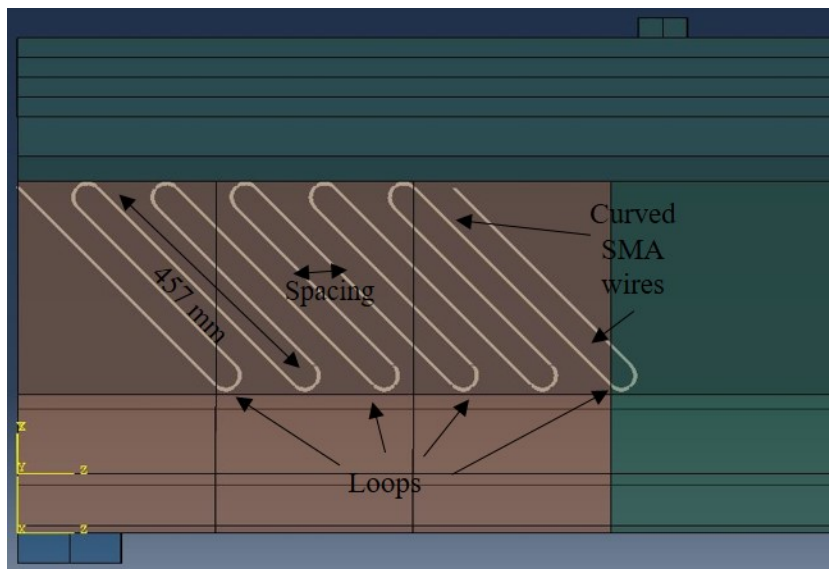


Fig. 15 Prestressed SMA repair

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RESULTS AND DISCUSSION

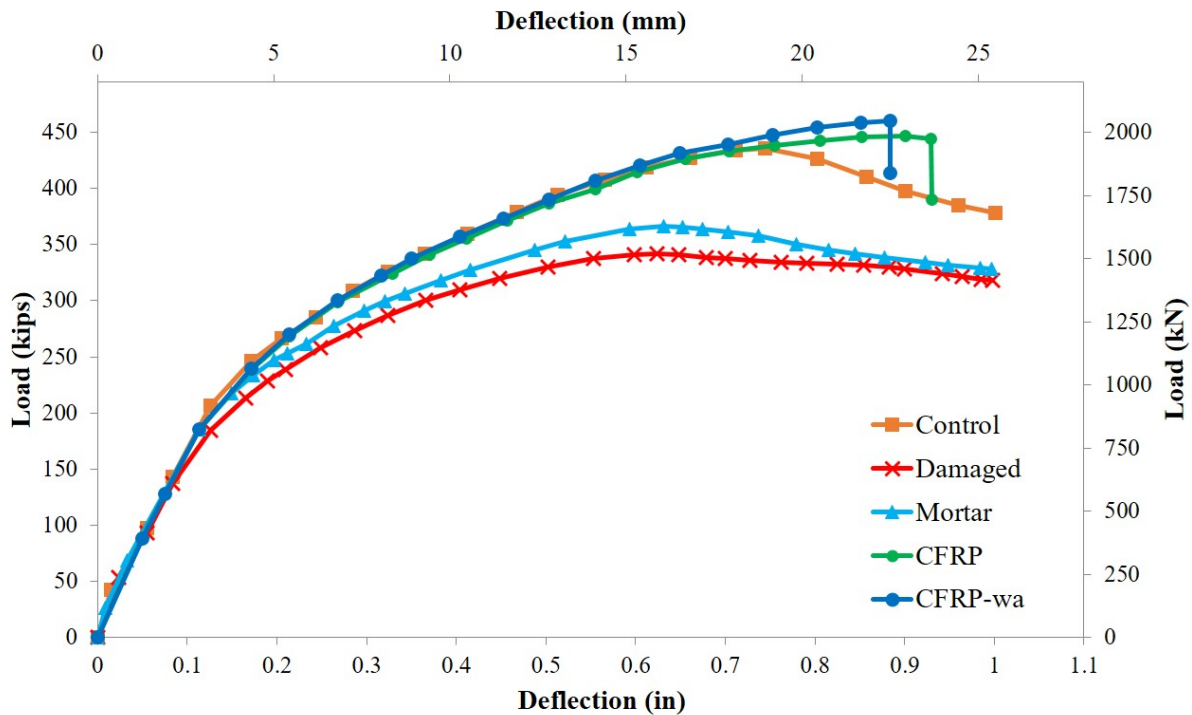
328 The numerical results including peak load, secant stiffness at deflection equal to 0.197 in. (5  
 329 mm) were summarized in Table 4. The load-deflection curve for mortar repair and CFRP  
 330 repair is illustrated in Figure 16.  
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Table 4. Finite element analysis results

Specimen	Peak load, kips (kN)	% of Control peak load	% of Control stiffness
Control	435.2 (1935.8)	100.0	100.0
Damaged	341.5 (1518.9)	78.5	88.9
Mortar	366.3 (1629.4)	84.2	94.4
CFRP	446.0 (1983.7)	102.5	97.3
CFRP-wa	459.4 (2043.5)	105.6	97.6
SMA-20	477.1 (2122.1)	109.6	121.5
SMA-10	434.4 (1932.3)	99.8	114.9

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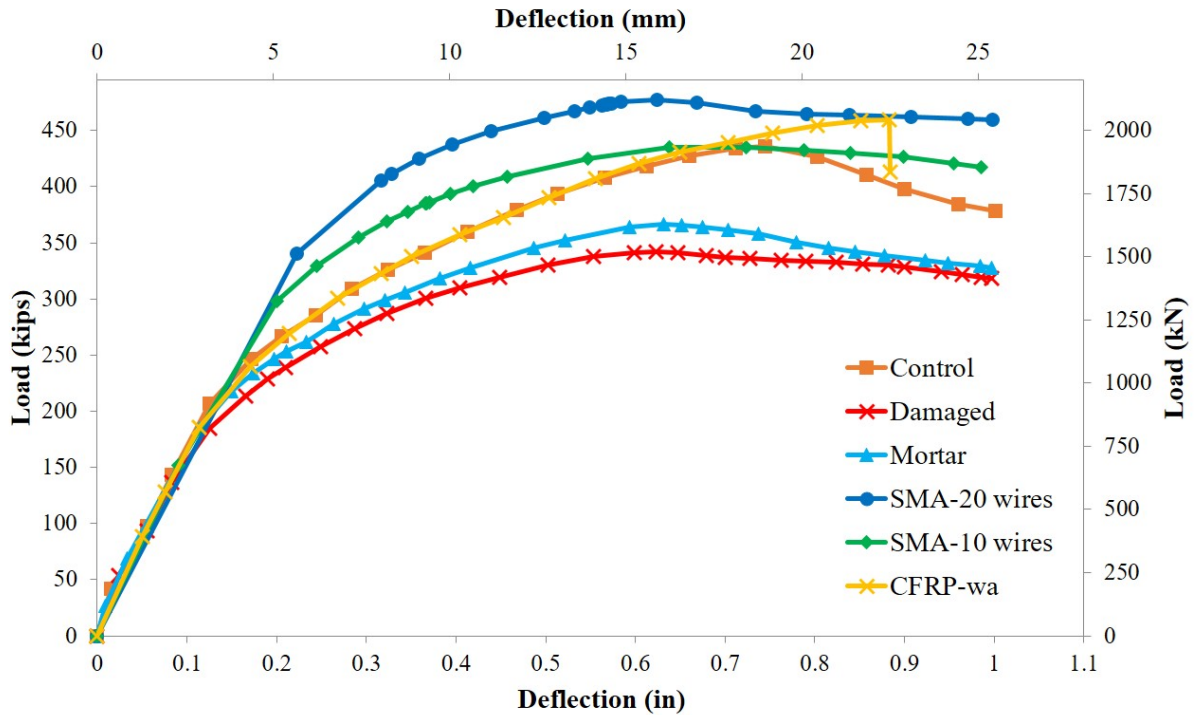
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Fig. 16 Load-deflection curve of FRP repair cases

337 From the figure, it is shown that mortar repair only showed 5.7% increase in peak force  
 338 and 5.5% increase in stiffness compared to damaged case, indicating that mortar alone is not  
 339 sufficient to restore the capacity of the girder. Both CFRP case and CFRP with anchor case  
 340 recovered the shear capacity of the girder. The peak force is increased by 24.0% and 27.1%  
 341 for CFRP and CFRP-wa, respectively. Compared to CFRP case, CFRP repair with longitudinal  
 342 anchors showed 3.1% increase in peak force and proved the effectiveness of strip anchors.  
 343



344 Fig. 17 Load-deflection curve of FRP and prestressed SMA repairs

347 Load-deflection curve of prestressed SMA repair is illustrated in Figure 17. From the  
 348 curves, it is observed that both SMA repair cases restored the peak force of the girder. More  
 349 importantly, compared to control case the stiffness is increased by 21.5% and 14.9% for 20  
 350 wires case and 10 wires case, respectively. The stiffness is even higher than that of CFRP-wa  
 351 repair. This is because the SMA prestressing was effectively able to delay the development  
 352 of shear cracks in the web. The results indicate that applying prestressing in the web is  
 353 effective in regaining strength and stiffness of the girder with end damage.  
 354

355 **CONCLUSIONS**

356 In this study, three-point bending tests were performed on prestressed beams with damaged  
 357 ends. Repair with mortar alone and mortar combined with externally bonded FRP laminates  
 358 was conducted. A FE model of a full-scale prestressed I-girder was generated using different  
 359 repair schemes were also explored. Based on the experimental and numerical results above, it  
 360 is shown that a mortar repair alone is not sufficient to regain the strength and stiffness of  
 361  
 362

363 girders with severely damaged ends. With additional externally bonded shear FRP sheets, the  
364 shear capacity of the prestressed girder with damaged end could be restored. Longitudinal  
365 anchors have been proven to be effective in preventing complete delamination of FRP  
366 laminates. To increase the effectiveness of GFRP repair, a stronger anchorage system is  
367 needed. From numerical results, it was shown that embedded prestressed SMA wires were  
368 effective in repairing the damaged end, especially in increasing the stiffness of the damaged  
369 girder.

370

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## 372 REFERENCES

373

374 1. ARTBA, <http://www.artba.org/economics/2016-u-s-deficient-bridges/>, 2016.

375 2. Alkhrdaji, T., “Strengthening of Concrete Structures Using FRP Composites”,

376 *STRUCTURE magazine*, June 2015.

377 3. Tedesco, J.W., Stallings, J.M., and EL-Mihilmy, M., “Rehabilitation of a Reinforced  
378 Concrete Bridge Using FRP Laminates”, RP 930-341; Highway Research Center, Auburn  
379 University, Auburn, AL, 1998.

380 4. Nanni, A., “Strengthening of an Impact-Damaged PC Girder,” *Concrete Repair Bulletin*,  
381 May-June 2004.

382 5. Carmichael, B.M., and Barnes, R.W., “Repair of the Uphapee Creek Bridge with FRP  
383 Laminates”, RP 930-466; Highway Research Center, Auburn University, Auburn, AL, 2005.

384 6. ElSafty, A., and Graeff, M.K., “The Repair of Damaged Bridge Girders with Carbon-  
385 Fiber-Reinforced Polymer “CFRP” Laminates”, BDK82 977-03; School of Engineering,  
386 University of North Florida, Jacksonville, FL, 2012.

387 7. Belarbi, A., Bae, S., Ayoub, A., Kuchma, D., Mirmiran, A., and Okeil, A., “Design of FRP  
388 Systems for Strengthening of Concrete Girders in Shear,” Research Report No. 678;  
389 NCHRP, 2011.

390 8. Abaqus 6.13, SIMULIA by Dassault Systèmes, software available at  
391 <https://www.3ds.com>.

392 9. Andrawes, B., and Pozolo, A., “Transfer and Development Lengths in Prestressed Self-  
393 consolidating Concrete Bridge Box and I-girders”, Research Report No. ICT-11-092;  
394 University of Illinois at Urbana-Champaign, Urbana, IL, USA, 2011.

395 10. QuakeWrap, “Product Data Sheet: QuakeWrap TU27C Carbon Fabric for Structural  
396 Strengthening,” QuakeWrap Inc.; Tucson, AZ, USA, 2016.

397 11. Shin, M., and Andrawes, B., “Experimental Investigation of Actively Confined Concrete  
398 Using Shape Memory Alloys,” *Engineering Structures*, V. 32, No. 3, November 2009, pp.  
399 656-664.